

# Cryptographic Group Actions and Digital Signatures

MsC Thesis supervised by Michele Battagliola, Alessio Meneghetti,  
Edoardo Persichetti  
defended at Università di Trento

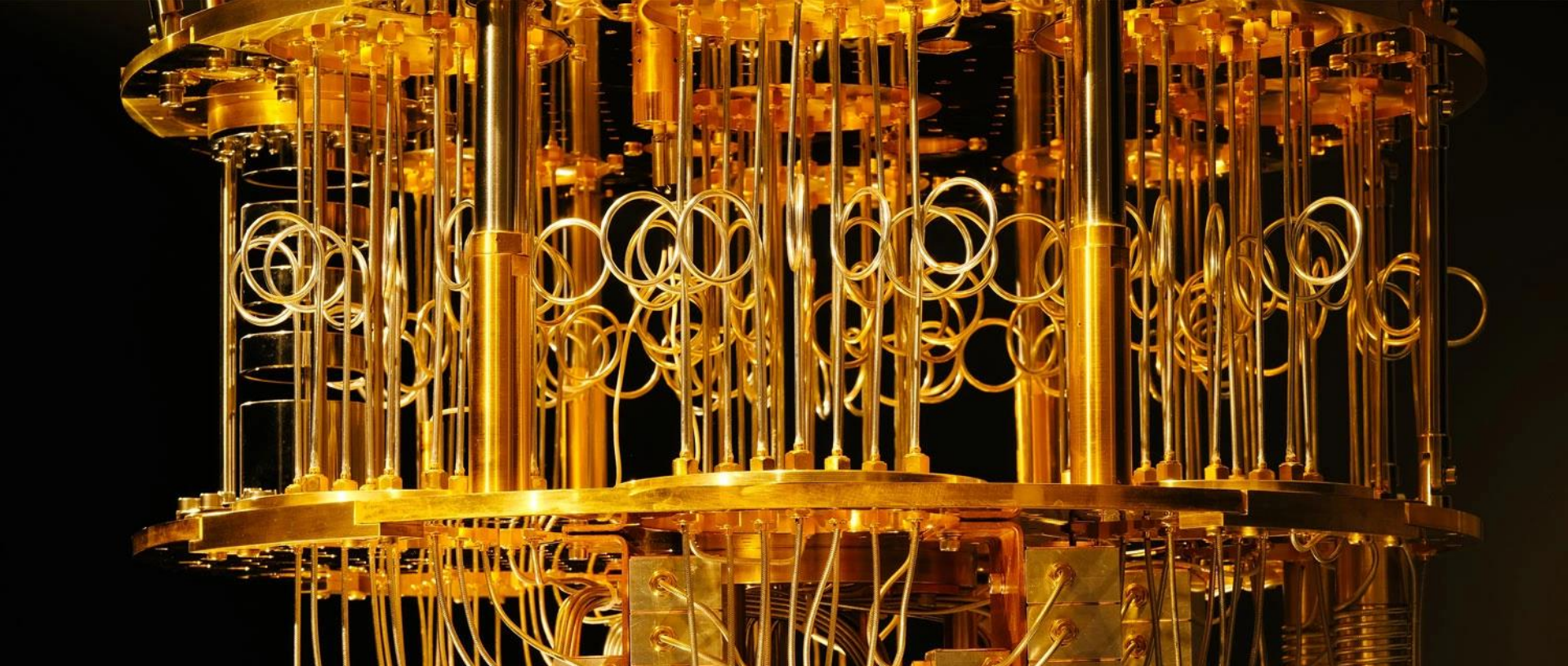
Giacomo Borin  
IBM Research Zurich & University of Zurich

**Opinions are my own!**



Universität  
Zürich<sup>UZH</sup>





Quantum Computers represents an existential threat to existing Cryptographic Infrastructure

# Post Quantum Cryptography

200\* > people start researching

2016 > NIST opens PQC call

2024 > FIPS 203 – 204 – 205

202\* > Ongoing Signature  
'on ramp' call & more

There is  
still a lot  
of work

# Discrete Logarithm Problem

$x$

$\rightarrow$

$g^{**x} \% N$

$pk$

$sk$

# Discrete Logarithm Problem

KEM, DS,

NIKE, Commitments, OT, RS,  
OPRF, MPC, IBE...

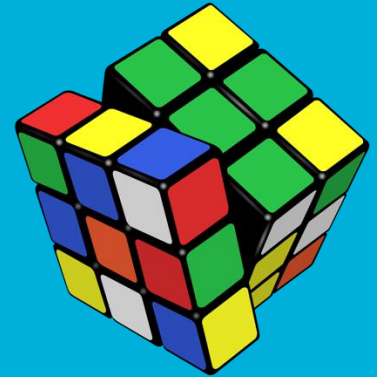
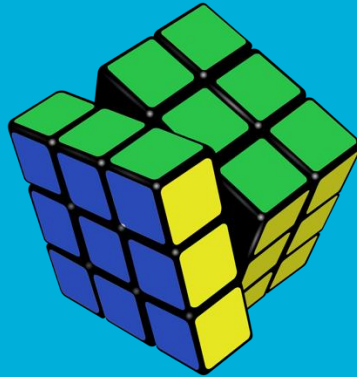
# Discrete Logarithm Problem

$$\begin{aligned} & (g^{**x} \% N) * (g^{**y} \% N) \\ & = \\ & g^{**(x+y)} \% N \end{aligned}$$

# Cryptographic Group Actions

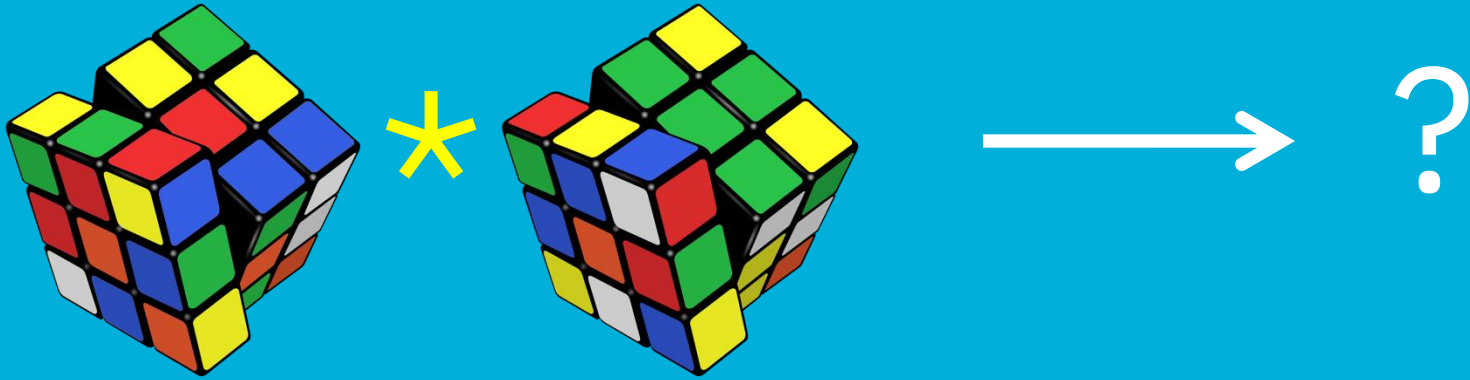
FBBDL  
RRDD  
UUF...

\*





# Cryptographic Group Action



# Group Actions to Digital Signatures



FBBDLRRDDUUF...



DRFULBULFDRL...  
 FLDLRLUBBRD...  
 RDUUFFLRLUUD...

$$\text{SHA3}(\text{Cube}_1 \text{ } \dots \text{ } \text{Cube}_n, *) = 01 \dots 0$$

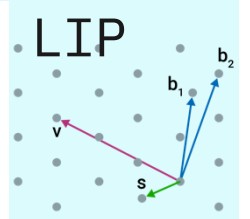
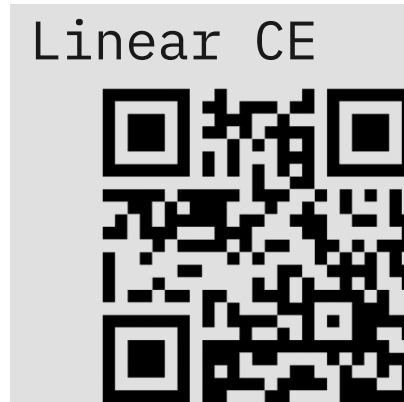
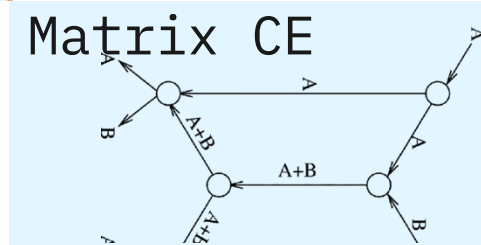
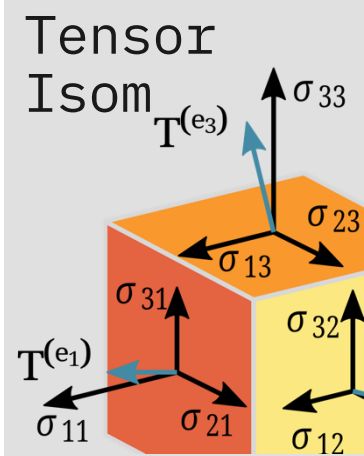
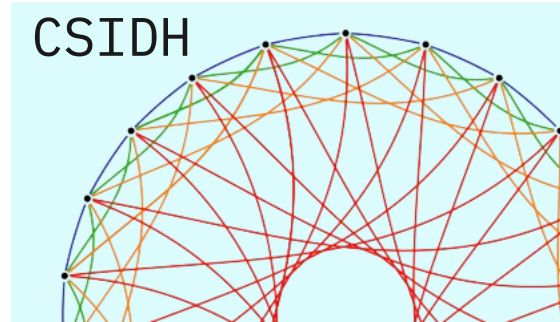
BBUFDLRRFLBB...

Stolbunov, Anton. "Cryptographic schemes based on isogenies." (2012).

Jean-Marc Couveignes. Hard homogeneous spaces. Cryptology ePrint Archive, Report 2006/291, 2006

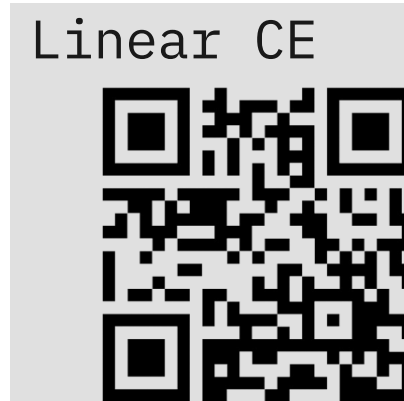
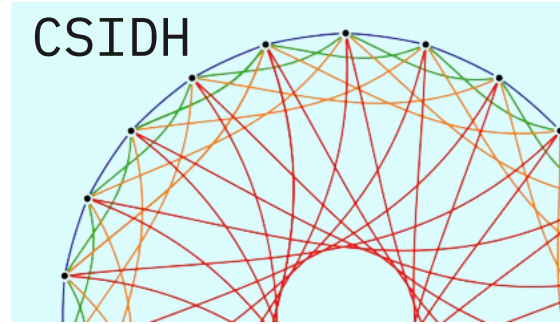
# Cryptographic Group Actions

- Digital Signatures
- Ring S.
- Threshold S.
- *Blind S.-ish*
- Bit Commitments
- KEM
- NIKE
- OT



# Cryptographic Group Actions

- Crtyptanalysis
- Improving efficiency (smaller and faster)
- New Constructions
- New Group Actions (?)



[gbor.in/msctthesis](http://gbor.in/msctthesis)

